

Boosting Classifiers for Weed Seeds Identification

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ABSTRACT

The identification and classification of seeds are of major technical and economical importance in the agricultural industry. To automate these activities, like in ocular inspection one should consider seed size, shape, color and texture, which can be obtained from seed images. In this work we complement previous studies on the discriminating power of these characteristics for the unique identification of seeds of 57 weed species. In particular, we discuss the possibility of improving the naïve Bayes and artificial neural network classifiers previously developed in order to avoid the use of color features as classification parameters. Morphological and textural seed characteristics can be obtained from black and white images, which are easier to process and require a cheaper hardware than color ones. To this end, we boost the classification methods by means of the AdaBoost.M1 technique, and compare the results obtained with the performance achieved when using color images. We conclude that boosting the naïve Bayes and neural classifiers does not fully compensate the discriminating power of color features. However, the improvement in classification accuracy might be enough to make the classifier still acceptable in practical applications.

Key words: machine vision; classification; boosting; neural networks

1. INTRODUCTION

Reliable and fast identification/classification of seeds is of major technical and economical importance for the agricultural industry. Common practices based on specialized technicians are slow, have low reproducibility, and possess a degree of subjectivity hard to quantify. Machine vision seems a suitable technique to automate this task, since numerous image-processing algorithms are available for extracting classification features from seed images. Like in the standard ocular identification, automatic classification should be based on knowledge of seed size, shape, color and texture (i.e., greytone variations on the surface, see [13],[10])

Most previous attempts to identify seeds by machine vision have concentrated on cultivated varieties [4,8,16,17,18,19,21,23,24]. In these studies image analysis was essentially restricted to basic geometrical measurements to obtain different parameters (shape factor, aspect ratio, length/area, etc.). In addition, color was successfully used to separate red-, amber- and white-colored wheat. More recent studies have used color images to establish seed quality and hardseededness of some annual pasture legumes[15], to characterize fungal damage, viral diseases and immature soybean seeds[1], etc.

Besides varietal identification and cereal grain grading, early identification of weeds from the analysis of strange

seeds is also of major interest in the agricultural industry. This can be done for the purpose of chemically controlling weed growth or, as occurs in many countries, it can be routinely performed as part of official requirements before a seed batch can be made commercially available (purity analysis). In particular, Argentina's law regulations require the analysis by registered laboratories of a small batch sample before a seed batch can be made commercially available. In these analyses, commercial and strange seeds present are separated, and the latter ones identified one by one. The studies in the present work are part of a development to avoid the continuous training of new technicians to perform this task, providing an automatic classifier that can be used by less skilled operators. Weed seeds are also identified by seed testing stations and seed corporations to measure the purity of the harvest, and by research stations to detect changes in seed banks in the soil. Another possible application is the identification of very strange seeds in botanical gardens, although this would require a very large database.

An early attempt to identify weed seeds[20] showed the importance of using color instead of black and white images to improve classification accuracy. More recently, Chtioui *et al.*[5] compared the capabilities of linear discriminant analysis and artificial neural networks (ANNs) to identify weed seeds from morphological and textural parameters. However, these investigations considered only four different species, which does not provide a good characterization of inter-species seed variations. In previous works[11,12], we assessed the discriminating power of different seed characteristics for the unique identification of seeds of weed species. We used a simple Bayesian approach (naïve Bayes classifier) to evaluate morphological, color and textural characteristics measured from video images, establishing their importance as classification features for weed seeds identification. The final classifier based on the optimal set of features showed a remarkable good performance. In addition, we presented classification results obtained using the same feature set as input of a committee of ANNs. These preliminary studies were conducted on a much larger basis than previous ones[5,20], including seed images of frequent weeds found in Argentina's commercial seed production industry. In particular, to avoid introducing a bias in the selection of species considered, we restricted ourselves to the 58 species listed by the Secretary of Agriculture as prohibited and primary- and secondary-tolerated weeds. From this list we finally considered 57 species for which a good number (~ 40) of young exemplars were available in the seed bank of the Seed Analysis Laboratory at the Oliveros Experimental Station of the National Institute for Agricultural Technology (INTA).

In this work we complement our previous study on automatic seed identification. In particular, we explore the possibility of improving the classifiers developed in [11,12] in order to achieve similar identification capabilities without using the color variables as classification features. For this, we use the standard boosting algorithm AdaBoost.M1 [9]. This goal points to avoiding the use of color images, which would simplify the hardware requirements for a commercial system with the concomitant reduction in cost and operational complexity (black and white cameras and image acquisition boards are much cheaper than RGB ones, control of illumination conditions is far less important in processing gray-tone images than color ones, etc.).

This work is organized as follows. In Section 2 we briefly describe the image acquisition and feature selection processes, and summarize the results obtained in our preliminary works [11,12]. In Section 3 we introduce the boosting algorithm AdaBoost.M1, and discuss the efficiency of the boosted classifiers based only on morphological and textural seed characteristics. Finally, in Section 4 we summarize our work and draw some conclusions.

2. FEATURE EXTRACTION AND CLASSIFICATION

Image Database and Feature Extraction

We have built a database containing 3163 images of the 57 species considered (a list of these species is available on request). Details on the experimental settings used to capture these images can be found in [12]. They consist of 768×512 pixel arrays whose entries are 24-bit records, corresponding to the 256 pixel intensity levels (8 bits) for each of the red (*R*), green (*G*) and blue (*B*) channels.

From the raw seed images we selected nearly optimal sets of 10 morphological, 7 color and 7 textural features to be used as classification parameters. For this selection we implemented standard sequential forward and backward algorithms [14], using the performance of a naïve Bayes classifier as the selection criterion. This classifier fits the class conditional probabilities with a product of distributions of the individual features—we used Gaussian distributions in this implementation—and, in spite of this simplification, it performs well on the problem at hand (see below). The same selection procedure applied to the 24 parameters as a whole

retained an optimal set of 12 (6 morphological, 4 color and 2 textural) features, which were finally used to build the classifiers. A description of these parameters and the selection algorithm can be found in [12]. In this work, in building the boosted classifiers we will consider the original 10 morphological and 7 textural features to evaluate the possibility of disregarding color information.

Discriminating power

In [11,12] we have compared the discriminating power of different sets of features using naïve Bayes classifiers. We found that the largest discriminating power corresponds to morphological features, while color and texture characteristics are not very good as classification parameters. Furthermore, the best generalization results for a combination of two type of characteristics corresponds to morphology plus color (see Table 2 in [12]). However, the use of morphology and texture would require considering only black and white images, which, as stated in the Introduction, constitutes an important simplification and a reduction in hardware cost.

For the sake of comparison with the results obtained in this work (see Section 3), in Table 1 we reproduce the performances obtained in [12] using naïve Bayes classifiers built in terms of the optimal set of 12 features. Figures in this table are the averages and standard deviations over 30 independent experiments. In each experiment we have split the 3163 images of the 57 species considered in training and test sets, randomly choosing, for each species, 80% of the images to build the classifier and including the remaining 20% in the test set. This leaves 2530 images for training and 633 images for testing the system. Table 1 gives the average performances and standard deviations for both the training and test sets. It also shows how performance increases when the system assigns a test image to any of the *n* most probable classes. The different cases considered are indicated in the table as First Option (*n*=1, standard classification), First Two Options (*n*=2) and First Three Options (*n*=3). Notice that for *n* > 1 the classification is considered as correct if the test image corresponds to any of the *n* classes with the largest probabilities. This possibility is very useful in practice, since untrained operators can easily select the correct option by simple visual comparison with stored representative seed images of the *n* classes suggested by the classifier.

Table 1: Performances of different classifiers as percentage of correct seed identifications using the optimal set of 12 features. Mean values and standard deviations are estimated from 30 independent experiments, as described in the main text.

Classifier	First Option		First Two Options		First Three Options	
	Training	Test	Training	Test	Training	Test
Naïve Bayes	97.5 ± 0.2	95.8 ± 0.9	99.4 ± 0.1	98.7 ± 0.4	99.7 ± 0.1	99.2 ± 0.3
Single ANN	100	95.6 ± 0.8	100	98.6 ± 0.4	100	99.4 ± 0.3
Committee	MR	100	100	98.3 ± 0.5	100	98.5 ± 0.4
	AP	100	100	99.0 ± 0.5	100	99.5 ± 0.3

Neural network classifier

To compare with the naïve Bayes classifier, in [11,12] we have also developed classifiers based on ANNs [2]. For

this we used the same feature set selected in the Bayesian approach, and trained feedforward networks with 12 input, 40 hidden, and 57 output units. We employed

output units with softmax (normalized exponential) activation functions to allow the interpretation of outputs as class probabilities. Furthermore, a cross-entropy error measure was used, which is the standard choice for classification problems. We trained the ANNs with the usual backpropagation rule until convergence, since only negligible overfitting problems were observed. This avoided the use of part of the training set for validation purposes (except for the initial selection of the optimal number of hidden units).

The performance of a single (generic) ANN and the results obtained in [12] by structuring 10 networks in a committee are reproduced in Table 1. In the case of the ANN committee we considered two options: i) each network votes for the class with the largest probability according to its own outputs, and the image is finally assigned to the class with the majority of votes (Majority Rule, MR), and ii) the class probability outputs from the 10 networks are added and the image is assigned to the class with the largest sum value (Added Probabilities, AP). Again in this case, all the results quoted correspond to an average over 30 independent realizations of the whole procedure.

A complete comparative description of the different methods' performances is given in [12]. Using standard paired *t*-tests, the results show that the two ANN committee implementations are better than the naïve Bayes and single ANN classifier with more than a 99% confidence level. Moreover, the strategy of adding

probabilities in the committee is better than the majority-rule vote with a confidence level also above 99%. We note, however, that there are risks in applying the paired-difference *t*-test to different random train-test splits of the data[7].

Several comments are in order at this point. First, we stress the excellent performance of the naïve Bayes classifier, which might be related to an effective near independence of the selected classification parameters. Secondly, since in the ANN approach the performance of a single network is already very good, there is little room left for improvement by adding several predictors in a committee. Notice that when the system is allowed to suggest three options for class membership, from the 633 images in the test set only 5 images are misclassified by the naïve Bayes approach and 4 images by the single ANN (for both methods the performance reaches 100% with five options). Of course, for a much larger number of species the classification problem would be more demanding and the ANN committee might have an edge over other simpler methods. Furthermore, feature selection should be performed using this classifier as selection criterion to obtain an optimal set for the ANN approach. In passing we mention that there are more sophisticated feature selection methods than the one implemented in this work[6,14]. Finally, we stress the fact that different realizations of training and test sets do not substantially change performances, as indicated by the low standard deviations observed in the 30 independent runs.

AdaBoost.M1 Algorithm

Input: Data set $D = \{(x_i, y_i), i=1, m\}$, where $x_i \in X$ and $y_i \in Y = \{1, \dots, k\}$
 Base learning algorithm *WeakLearn*

Initialize: $w_i(1) = 1/m \quad \forall i=1, m$

For $t = 1$ to T :

- generate data set D_t by re-sampling m examples from D with probability $w_i(t)$
- train *WeakLearn* on D_t to obtain the base classifier $h_t : X \rightarrow Y$
- compute the error of h_t : $\epsilon_t = \Pr_{i \sim D_t} [h_t(x_i) \neq y_i]$; If $\epsilon_t > 1/2$ exit
- assign $\beta_t = \epsilon_t / (1 - \epsilon_t)$
- update distribution $w(t)$:

$$w_i(t+1) = w_i(t) \times \begin{cases} \beta_t & \text{if } h_t(x_i) = y_i \\ 1 & \text{otherwise} \end{cases}$$

- normalize distribution $w_i(t+1)$:

$$w_i(t+1) = w_i(t+1) / Z_t, \text{ where } Z_t = \sum_{i=1, m} w_i(t+1)$$

Output: Final hypothesis

$$h_{\text{Boost}}(x) = \operatorname{argmax}_{y \in Y} \sum_{t: h_t(x)=y} \log(1/\beta_t)$$

3. BOOSTING THE CLASSIFIERS: THE ADABOOST.M1 ALGORITHM

Boosting

Boosting is a general method to improve the performance of any learning algorithm that consistently generates classifiers with misclassification errors smaller than 50% on a given problem. The first effective boosting algorithm was developed by Schapire[22]; more recently, Freund and Schapire[9] introduced AdaBoost, a new

algorithm that has undergone intense theoretical study and empirical testing in the last years. In particular, in this work we will implement the simplest extension of AdaBoost to multiclass problems, the so called AdaBoost.M1 algorithm, whose pseudocode is given above.

AdaBoost.M1 takes as inputs a weak classification method (*WeakLearn*) and a dataset $D = \{(x_i, y_i), i=1, m\}$

with m examples, where $x_i \in X$ is an attribute vector and $y_i \in Y$ the corresponding class label (we will consider k classes). It calls repeatedly *WeakLearn*, applying, in each iteration t , this algorithm on a training dataset D_t obtained by re-sampling from D with probability $w_i(t)$. That is, *WeakLearn* finds a new classifier $h_t : X \rightarrow Y$ seeking to minimize the training error $\epsilon_t = \Pr_{i \sim D_t} [h_t(x_i) \neq y_i]$ (notice that the error is measured with respect to the distribution of examples in D_t). This process is iterated T times, and the hypotheses h_1, \dots, h_T obtained are combined in a final classifier h_{Boost} . The re-weighting of examples in D (starting from $w_i(t) = 1/m$) and the way of combining the successive hypotheses h_t are indicated in the algorithm's pseudocode above. Other boosting schemes change these particular rules. The idea behind boosting techniques is that "easy" examples that are correctly classified by most previous hypotheses get a small weight, while "hard" examples usually wrongly classified get larger weights. Thus, boosting concentrates the efforts of *WeakLearn* in those examples that are difficult to learn by this base algorithm. The final classifier is a weighted voting of the weak hypotheses obtained during the T iterations. The most important fundamental property of this technique is the fact that if *WeakLearn* has consistently errors $\epsilon_t < 1/2$, then the misclassification error of h_{Boost} on D drops to zero exponentially fast. Of course, this does not mean that the test error will be small. However, if T is not too large, theoretical and empirical investigations indicate that h_{Boost} may have very good generalization capabilities.

The main drawbacks of boosting are: 1) The base learner must produce hypotheses with misclassification errors $\epsilon_t < 1/2$. For random guessing among k classes the expected error is $1 - 1/k$, so that for $k > 2$ the requirement on ϵ_t can be difficult to achieve. Fortunately, for the problem under consideration in this work the weak classifiers we use (Naïve Bayes and ANN) have errors smaller than $1/2$ (see Fig. 2 below). 2) For very noisy datasets, containing many misclassified objects, the algorithm places too much attention on these wrong examples and the generalization performance deteriorates. In these cases regularization methods become necessary.

Alternatively, one may use a simpler committee method like *bagging*[3] (for *bootstrap aggregation*). Bagging simply trains T base classifiers on bootstrap re-samples of D , and outputs as final hypothesis

$$h_{\text{Bagging}}(x) = \operatorname{argmax}_{y \in Y} \sum_{t=1, T} \Pr[h_t(x)=y].$$

That is, it assigns instance x to the class with the largest added probability according to the T base classifiers. In the following we will use the performance of this committee method as an additional basis of comparison for the performance of the more sophisticated boosting algorithm.

As stated in the Introduction, we have boosted the base classifiers described in the previous section (naïve Bayes and ANN) without using the color features. For this we considered only the intensity $I=(R+G+B)/3$ instead of the three color channels, and initially used the 10 morphological and 7 textural parameters. In the case of the naïve Bayes classifier, we evaluated two standard ways of representing the class distribution of the individual features: i) by fitting a normal distribution, like

in Section 2, and ii) by using a discrete histogram and optimizing the number of bins. This last alternative gives more flexibility to the base classifier, allowing it to learn perfectly all the training examples after some rounds of the boosting algorithm. Although this seems to be preferable from a methodological point of view (no examples are "too hard" for the base classifier), we will see that overfitting problems deteriorate the final results. In Fig. 1 we give the misclassification error averaged over the 30 experiments, for the training and test sets, as a function of the number of ensemble members (equivalent to boosting rounds T). The training error plot shows, as salient feature, the flexibility of ANN and discrete naïve Bayes base learners, whose errors reach zero after some rounds of the algorithm. From the test error plot we see that boosting performs always slightly better than bagging for all learning algorithms, and that ANNs produce the best generalization results for this problem. A summary of the most relevant results is given in Table 2. In Fig. 2 we plot the error ϵ_t on the re-weighted training set D_t during the boosting process. We see that, for all base learners, ϵ_t stays below 0.5 as required, being particularly small for the oversized ANNs used that are able to fit even the hardest examples.

The means and standard deviations of the results obtained after 30 runs of AdaBoost.M1 are given in Table 2. For the sake of comparison, in this table we include also some of the results quoted in Section 2 without boosting the classifiers but using color images (first column). The results in the second column (under the title "Single") correspond to the average performances of the first classifiers obtained while running AdaBoost.M1 for each base learning method ($T=1$). The third column in Table 2 gives the results of simply bagging 20 classifiers, and the last column contains the results of AdaBoost.M1 with $T=20$. A larger number of iterations of the algorithm does not lead to a sensible improvement in the final results. Notice that: i) Comparison of the first, second and fourth columns clearly shows that the performance of a single classifier improves via boosting, but this is not enough to regain the accuracy obtained with the inclusion of color features. ii) Although the AdaBoost.M1 algorithm produces the best black-and-white images classifiers, the improvement over the standard classifiers and the simpler bagging approach is not substantial. This certainly points to the fact that, for this problem, the naïve Bayes and ANN approaches are already producing very good classifiers, without leaving much room for improvement. iii) The histogram implementation of the naïve Bayes classifier shows the largest improvement due to boosting. Unfortunately, this base learner has a poor performance due to overfitting and the boosted classifier does not reach a competitive performance.

As mentioned previously in connection with Table 1, instead of simply trying to identify the seed species one can let the system suggest several probable options to the operator, so that he/she can make the final decision. In this practical situation, boosted ANNs predict the correct species within three options with $(98.8 \pm 0.4)\%$ of accuracy. This performance might be acceptable for a commercial system, which opens up the possibility of adapting the existing software to work only with gray-tone images.

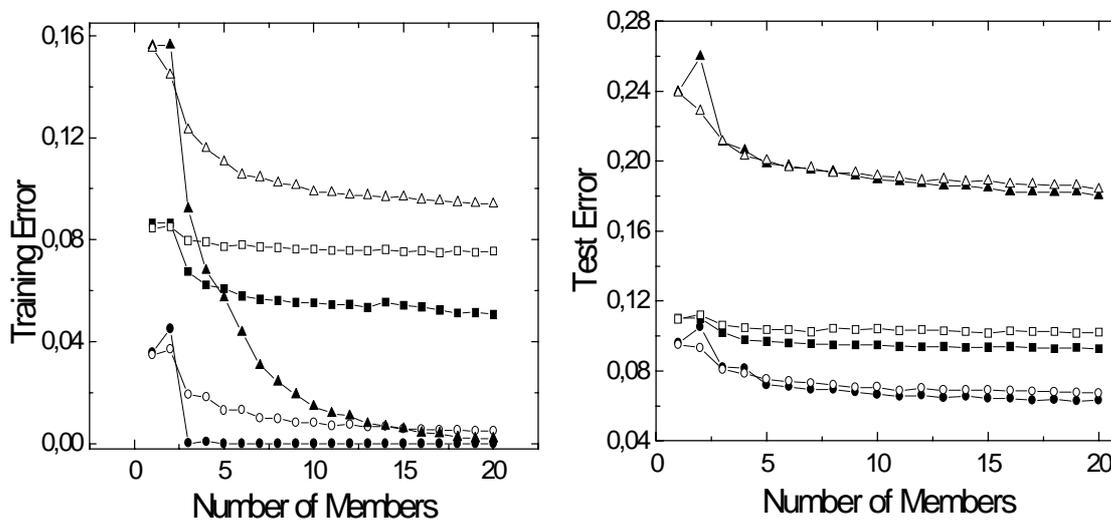
Table 2: Average test set results and corresponding standard deviations of 30 boosting experiments with $T=20$, for the base classifiers indicated and using black and white images. Also given for comparison the results corresponding to the standard (single) classifiers and 20 bagged base learners, and the performances obtained using color images.

Method		Color Images	Black and White Images		
			Single	Bagging	Boosting
Naïve	Gaussian	95.8 ± 0.9	89.0 ± 1.0	89.8 ± 1.1	90.7 ± 1.1
Bayes	Histogram	-	76.0 ± 2.3	81.6 ± 1.2	82.0 ± 2.0
ANN	Single	95.6 ± 0.8	90.4 ± 1.0	93.1 ± 1.0	93.7 ± 0.8
	Committee	96.6 ± 0.7	-	-	-

Table 3: Performances of different classifiers using the optimal set of 12 morphological plus textural features. Mean values and standard deviations are estimated from 30 independent experiments.

Method		First Option			First Three Options		
		Single	Bagging	Boosting	Single	Bagging	Boosting
Naïve	Gaussian	89.2 ± 1.1	90.2 ± 1.0	90.6 ± 1.0	98.0 ± 0.5	98.7 ± 0.4	97.7 ± 0.6
Bayes	Histogram	77.2 ± 2.0	82.3 ± 1.4	83.0 ± 1.9	93.2 ± 1.0	95.4 ± 1.1	94.5 ± 1.0
Single ANN		91.0 ± 1.2	93.8 ± 0.9	94.0 ± 0.8	98.2 ± 0.6	98.9 ± 0.4	98.9 ± 0.4

Fig. 1: Training and test errors as a function of the number of ensemble members. Full and open symbols indicate the results of boosting and bagging the base learners. Squares and triangles correspond to naïve Bayes with Gaussian distributions and discrete histograms respectively; circles are the results for ANN.



As a final investigation, from the 17 seed characteristics in black and white images we selected an optimal set of 12 (7 morphological and 5 textural) parameters, again using the Naïve Bayes classifier as selection criterion. Boosting this reduced set produced slightly better results, as shown in Table 3.

4. SUMMARY AND CONCLUSIONS

We have investigated the possibility of avoiding color features in the weed seed identification problem. For this, we improved the Bayesian and ANN methodologies

previously used in [11,12] by boosting them via the AdaBoost.M1 algorithm. The purposes of this work were simplifying operating conditions (illumination control) and reducing the cost of a potential commercial system based on the current development. The boosted classifiers based on gray-tone features (morphology and texture) were not able to achieve the same performance reached by the standard ones using color characteristics of the seeds. Notwithstanding this, the best result reported in Table 3 (94% of accuracy at first option and 98.9% of accuracy within three options) might well be acceptable in commercial applications.

For the number of species considered in this study, the preprocessing of images and the careful selection of measured features reduced considerably the complexity of the classification problem. However, one would expect this problem to become more demanding for databases containing several hundreds of species, as required in some applications. In such cases, the improvement of base classifiers via boosting might become more important. Work in this direction requires the lengthy acquisition of an extended database, which is currently in progress.

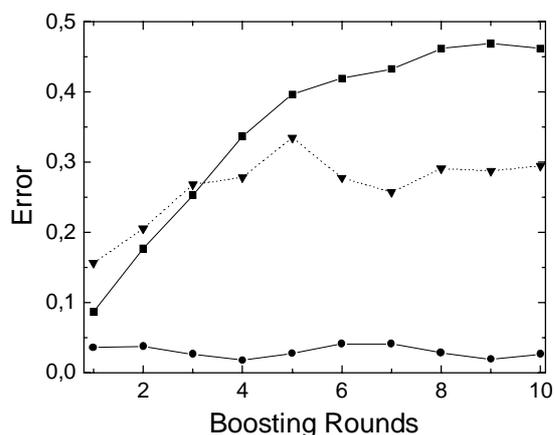


Fig. 2: Error ϵ_t evolution as a function of boosting rounds t , for different single base learners: Naïve Bayes with Gaussian distribution (squares), discrete histograms (triangles) and ANNs (full circles).

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